

# Precipitation Error Structure and Representation

Yudong Tian

University of Maryland & NASA Goddard Space Flight Center

## Collaborators:

Christa Peters-Lidard  
Ling Tang  
Ali Behrangi  
Bin Yong  
Huan Wu  
Kuo-lin Hsu  
Habib Emad

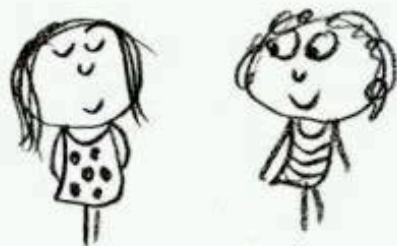
George Huffman  
Joe Turk  
Bob Joyce  
Sheng Chen  
Mathew Sapiano  
Takuji Kubota

Bob Adler  
John Eylander  
Pingping Xie  
Viviana Maggioni  
Xin Lin  
Tomoo Ushio

“Uncertainty is like happiness – everyone wants it, and everyone has their own idea of what it is.”

-- Y. Tian

# HAPPINESS IS



**...when someone says to you  
“You’ve lost weight”.**

## Outline

1. Precipitation errors are complex
2. Structure of precipitation errors
3. Communication of precipitation error and uncertainty

# 1. Precipitation errors are complex

## -- Physical

- \* Nonlinearity
- \* Intermittency
- \* Non-Gaussian

## -- Conceptual

sampling error, retrieval error, systematic error, random error, missed and false error, additive error, multiplicative error, type I error, type II error, signal, noise, ...

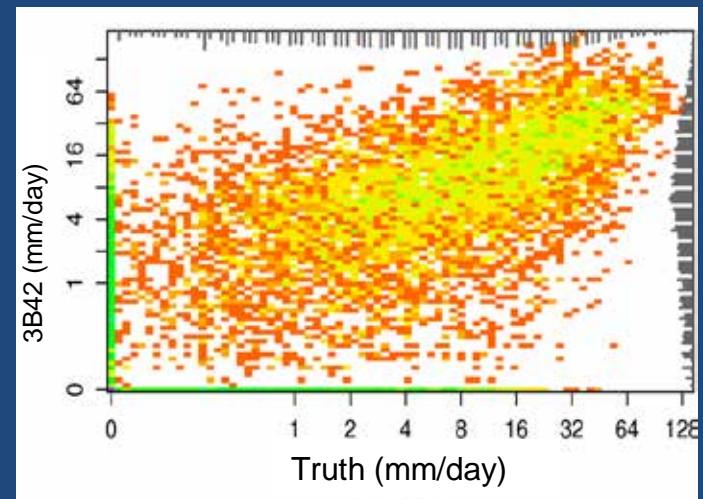
What do they do to uncertainty?

## 2. Error structure of precipitation measurements

Measurements

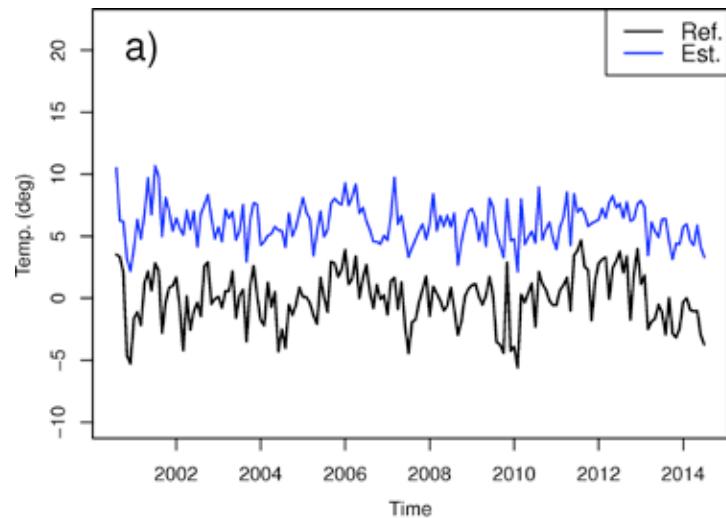


Truth

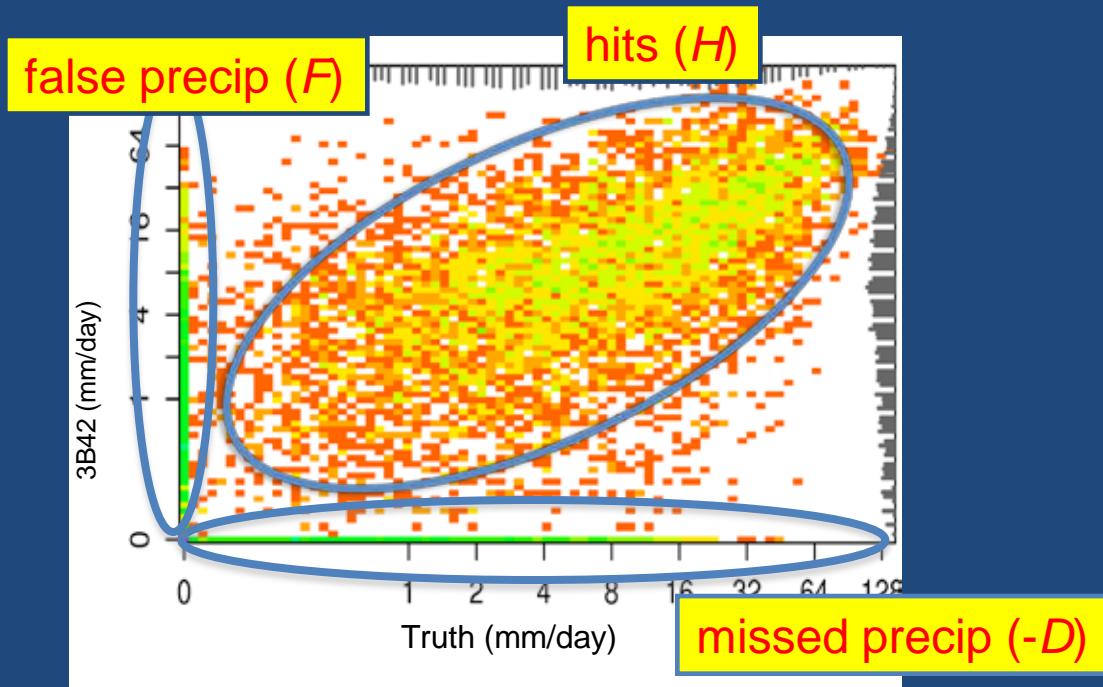


Measurements can be validated

## Conventional validation is not enough for error representation



Error comes in three components (Tian et al., 2009)



$$\text{(total error)} = \text{(hit error)} - \text{(missed)} + \text{(false)}$$
$$E = H - D + F$$

# New Error Decomposition Scheme

(total error)

$E$

(hit bias)

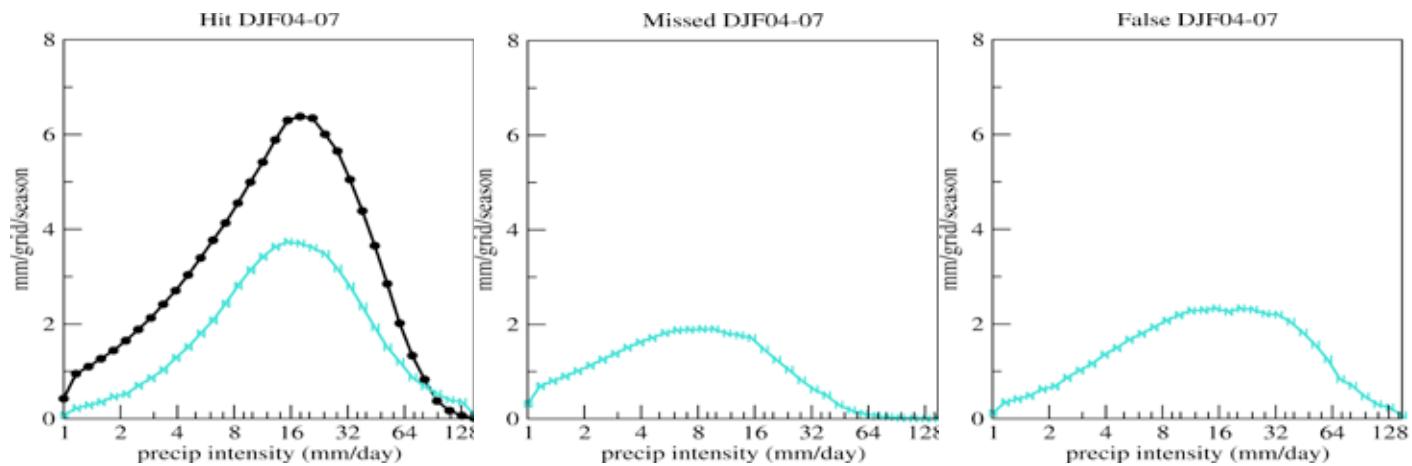
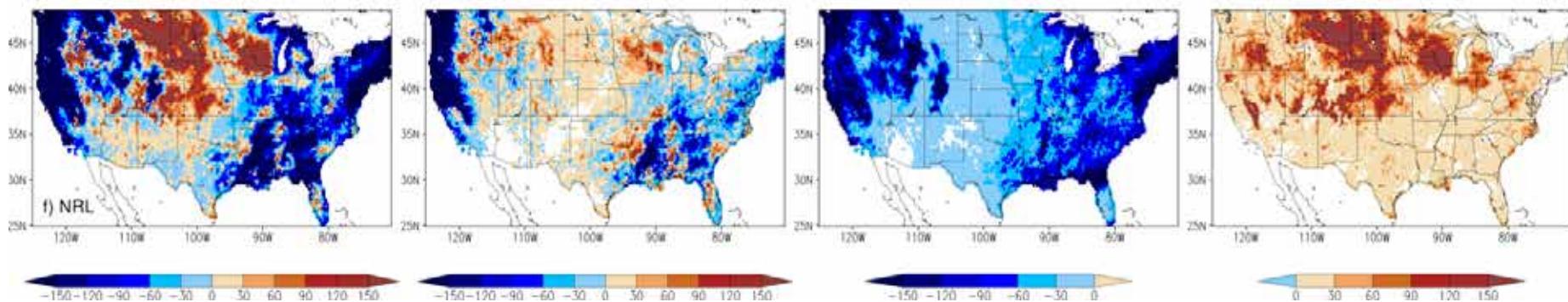
$H$

(missed)

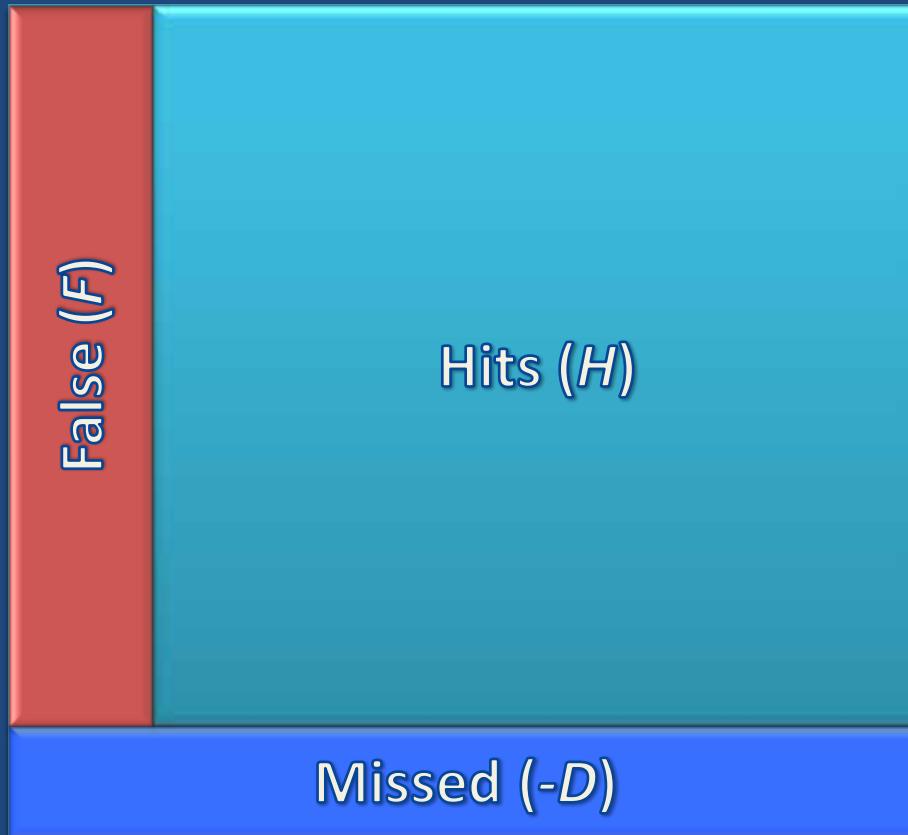
$D$

(false)

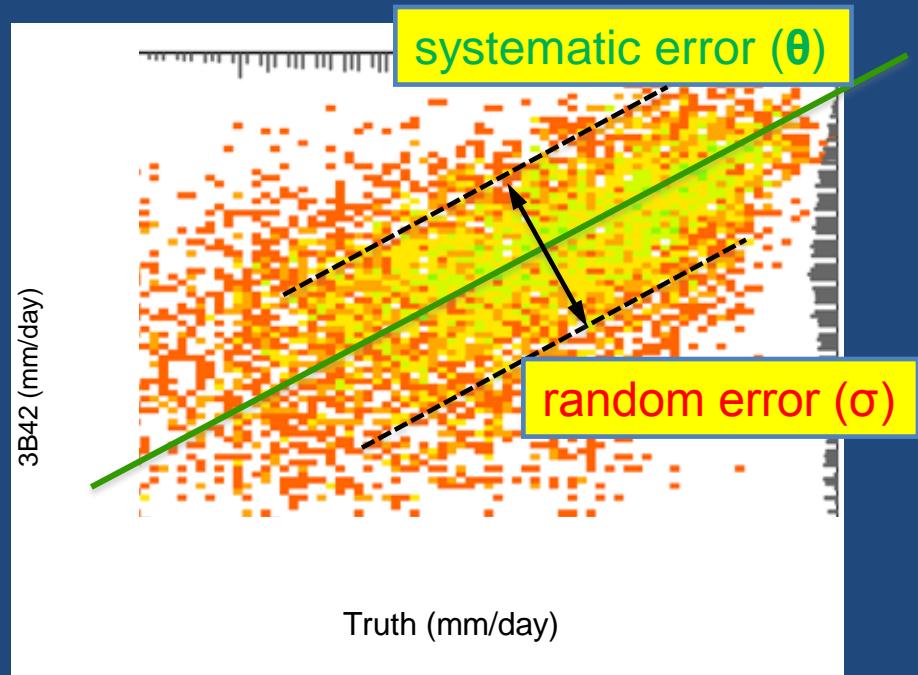
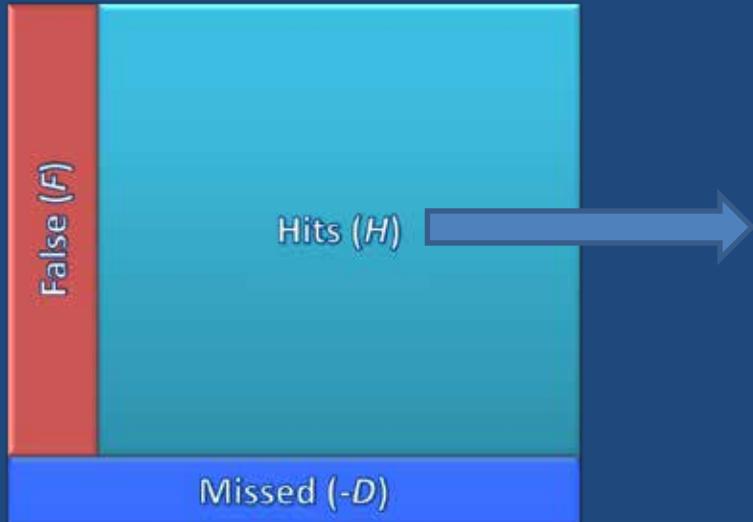
$F$



Precipitation error comes in three components



Each error component can be separated into systematic and random error



Epistemology of uncertainty

---

systematic error | random error

deterministic | stochastic

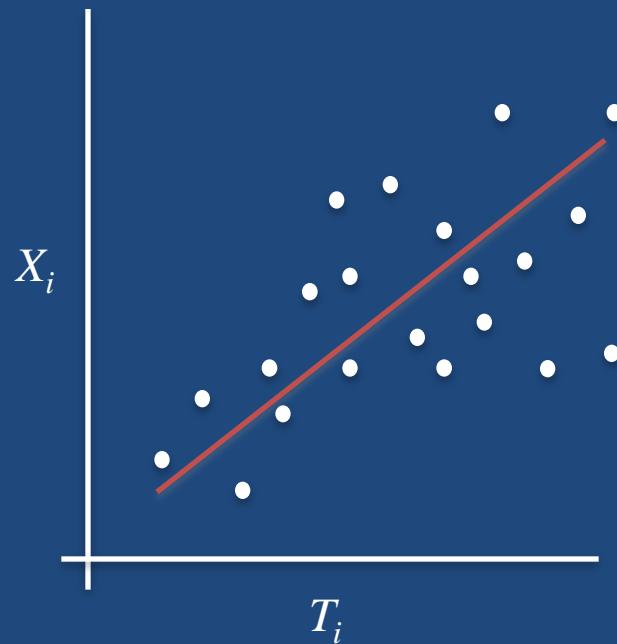
knowledge | ignorance

certainty | uncertainty

An error model is needed to separate systematic and random errors

Linear, additive error model

$$X_i = a + bT_i + e$$



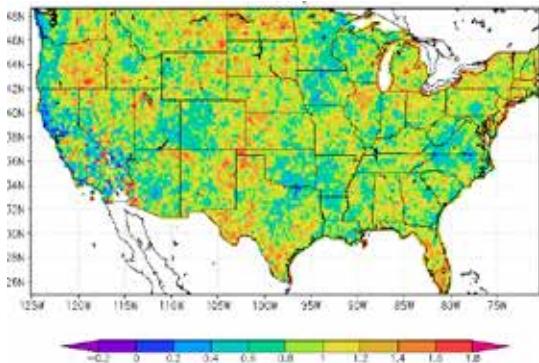
# Two parameters quantify systematic error

$$X_i = a T_i^\beta e^\varepsilon \quad \sigma = \text{stdev}(\varepsilon)$$

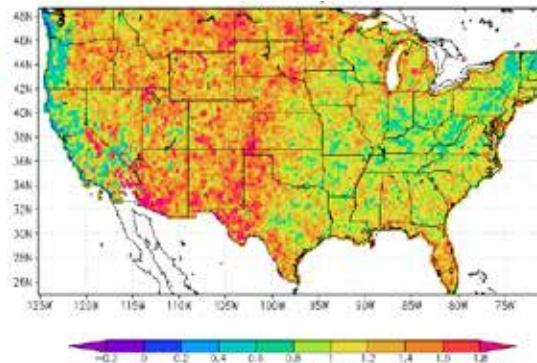
systematic error

$\alpha$ : scale error (ideal: 1)  
 $\beta$ : shape error (ideal: 1)

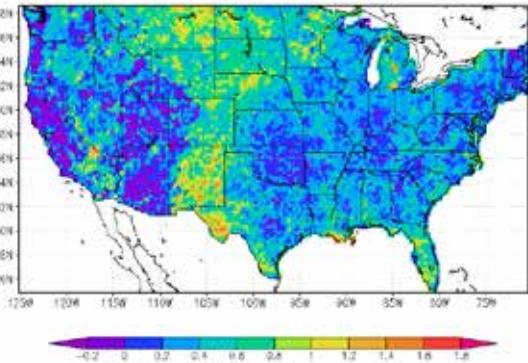
TMPA 3B42



TMPA 3B42RT

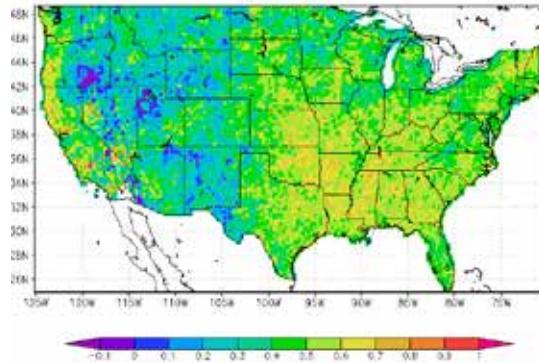


NOAA Radar

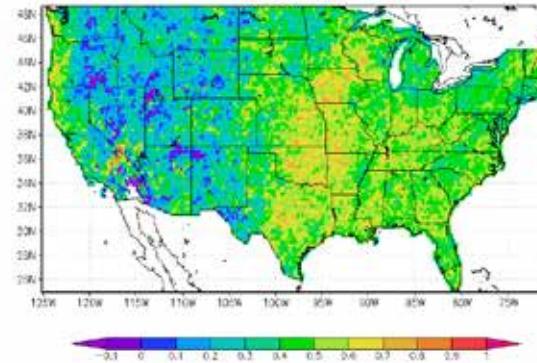


$\beta$

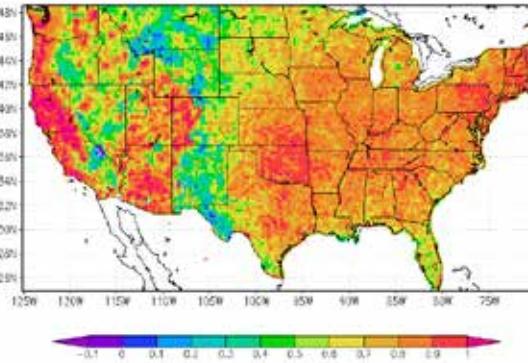
3B42 beta



3B42RT beta



STIV beta

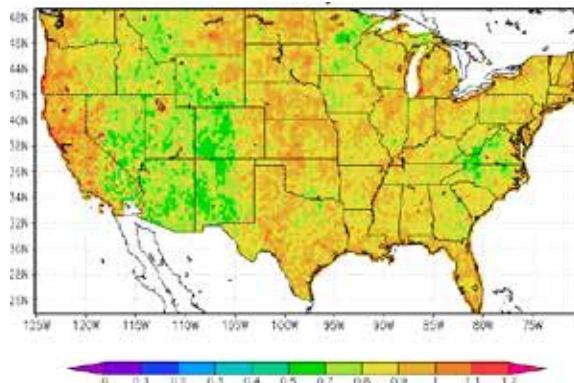


# One parameter quantifies random error

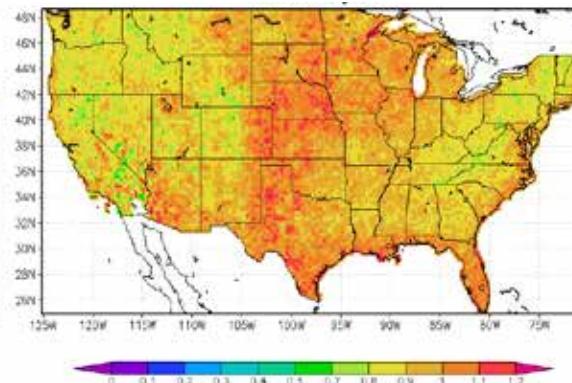
$$X_i = a T_i^\beta e^\varepsilon \quad \sigma = \text{stddev}(\varepsilon)$$

Random error  $\sigma$ : (ideal: 0)

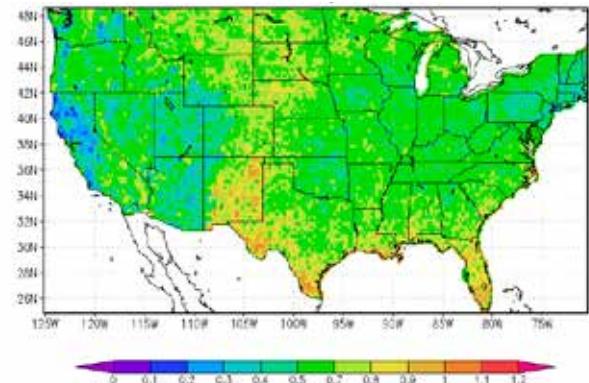
**TMPA 3B42**



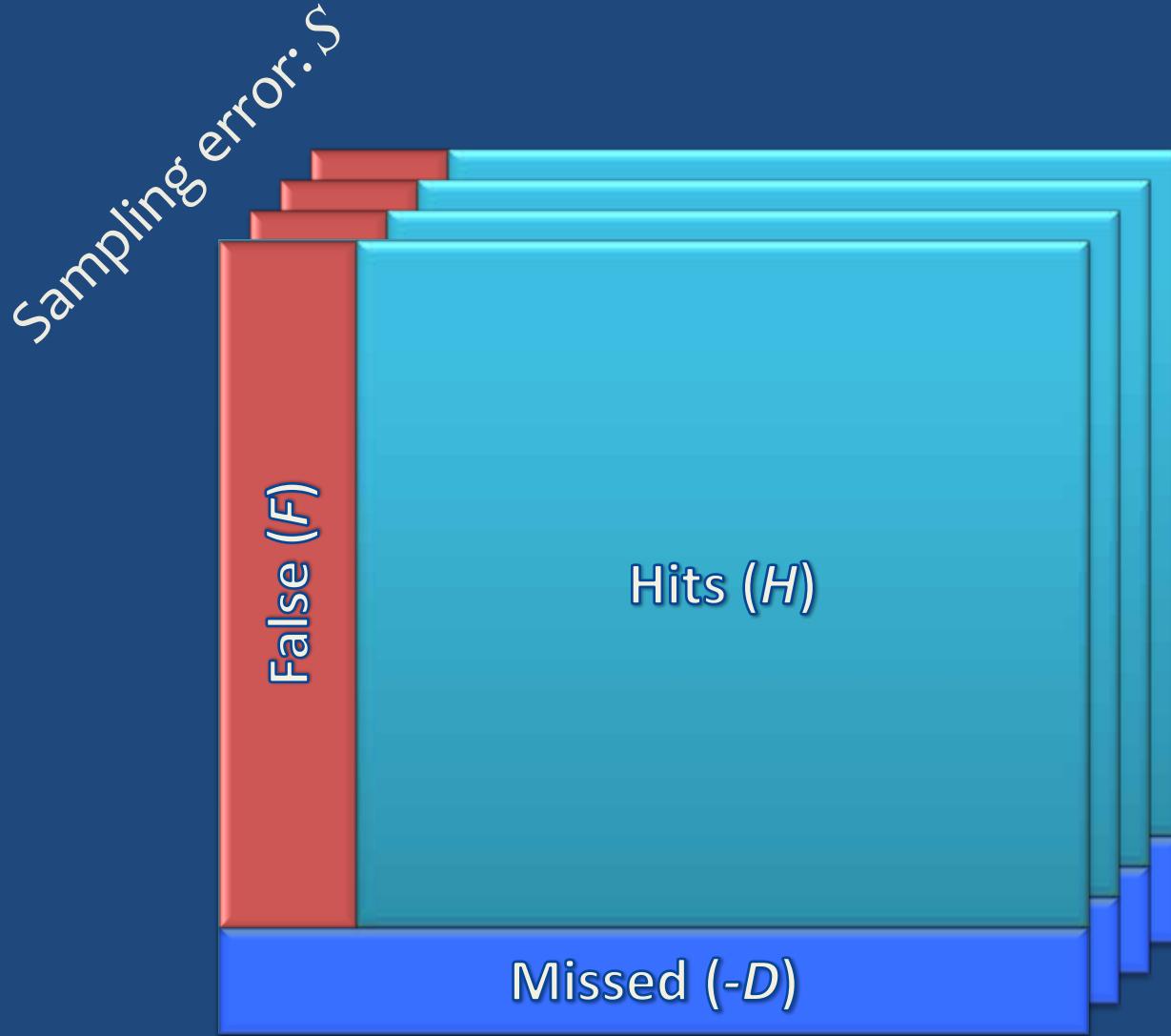
**TMPA 3B42RT**



**NOAA Radar**



Sampling error comes in when going from instantaneous to averages



Retrieval error: quantification = ( *-D, F, H* )

Error representation boils down to quantifying 3+1 components

Error type	Systematic	Random
Retrieval error	Hit error	$H=f(\alpha, \beta)$
	Missed	$-D$
	False	$F$
Sampling error	$g(H, -D, F)$	$\sigma_s$

### 3. Communication of precipitation error and uncertainty

-- Validation  $\neq$  error representation

Retrieval errors:

- Errors in precipitation come in components (H, -D, F)
- Each component has systematic and random errors
- Random errors define uncertainty
- Be explicit on error models used/assumed

Sampling errors:

- Estimating mean from discrete samples
- One more source of random errors

### 3. Communication of precipitation error and uncertainty

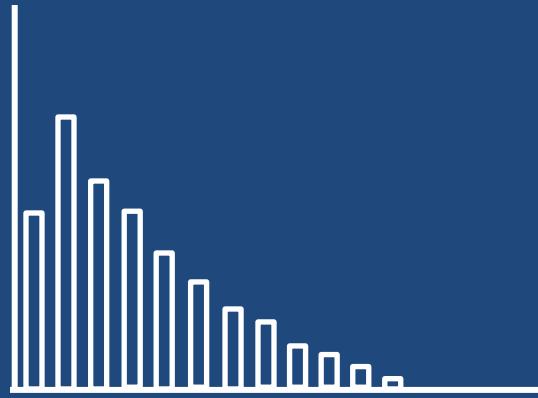
Questions for future studies:

- How to use the error structure for data assimilation/fusion?
- How detailed does error information have to be?

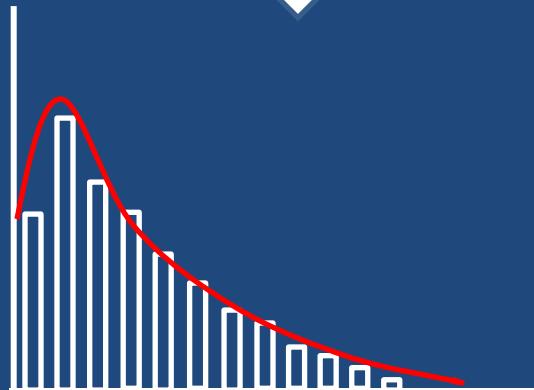
Can we simplify our message?

Error components		Selected references
Errors in precipitation	Sampling error	Laughlin (1981), Huffman (1997), Bell & Kundu (1996, 2000, 2003), Bell et al. (2001), Steiner et al. (2003), Nijssen & Lettenmaier (2004)
	Retrieval error	Arkin & Xie (1994), Smith et al. (1998), Adler et al. (2001), McCollum et al. (2002), McCollum & Ferraro (2003), Gottschalck et al. (2005), Hossain and Anagnostou (2006), Ebert et al. (2007), Tian et al. (2007), Tian & Peters-Lidard (2007), Lin & Hou (2008), Villarini et al. (2009), Sapiano & Arkin (2009), Tian et al. (2009, 2010), Tang et al. (2014)
	Random error	Villarini et al. (2009), Tian & Peters-Lidard (2010), Tian et al. (2013), Maggioni et al. (2014)

# Two schemes for random error representation



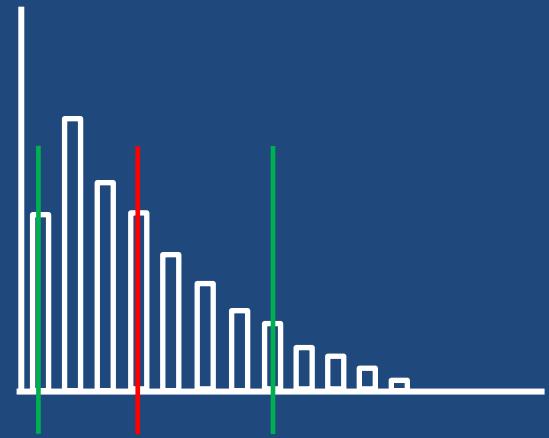
Parametric modeling



Non-parametric



Mean, median, percentiles, etc.



Error PDF with parameters  
( $\alpha, \beta, \sigma$ , etc...)

