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Absolute performance of drop size distribution fittings applied to 2DVD measurements from **GPM Ground Validation campaigns** E. Adirosi¹, E. Volpi², F. Lombardo², and L. Baldini¹

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Motivation

Modelling raindrop size distribution (DSD) is fundamental to develop reliable precipitation remote sensing products.

- Gamma distribution is the most widely used but other 2-parameter distributions have been proposed.
- At what extent assumptions of Gamma and other models are supported by disdrometer measurements ?

Objectives

- Gamma, lognormal, and Weibull distributions parameter) are (2 considered
- > Their absolute statistical performance in representing DSDs in nature is evaluated.
- > To provide some clues on the conditions under which a model is more **appropriate** to represent natural DSDs.

Methods

1. DSD definitions

a) Disdrometer measured

Product of the probability density function (pdf) of

2. Statistical inference of f(D) and $f_{v}(D)$

Gamma, lognormal, and Weibull distributions are fitted to

3. Model testing

The Kolmogorov-Smirnov (KS) test is used: a model assumption is accepted if

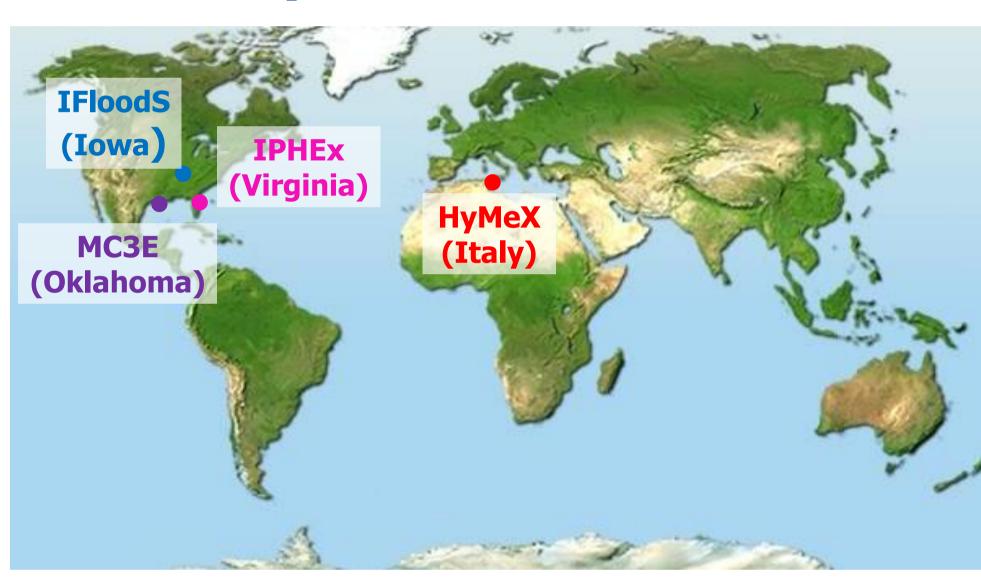
the 2DVD measured drop size spectra by the Maximum $D_M < \Delta_M(\alpha)$ drop diameters at ground f(D) by the number M of Likelihood Method (ML): where $\Delta_M(\alpha)$ is a critical reference value computed drops collected at ground through Monte Carlo simulations and a) Standard definition a) $\mathcal{L}(\beta,\gamma) = \prod_{i=1}^{n} [p(D_i;\beta,\gamma)]$ Product of concentration of raindrops in a volume of air n_c $D_M = max_i \left| F(D_i) - \hat{F}(D_i) \right|$ b) $\mathcal{L}(\beta,\gamma) = \prod_{i=1}^{i=1} [p(D_i;\beta,\gamma)]^{N_i}$ by the probability distribution of drop size in the For $f_{v}(D)$ fitting: unit volume of air $f_{v}(D)$ ($V = A \Delta t v(D)$) where Δt is the $\hat{F}_{V}(D_{i}) = \frac{1}{\sum_{z=1}^{M} 1/v(D_{z})} \sum_{i=1}^{l} \frac{1}{v(D_{i})}$ sampling time interval, A is the measuring area and v(D)is the terminal fall velocity of drops) : $N(D) = n_c f_v(D)$ where β and γ are the scale and shape parameters and N_i f(D) and $f_{\nu}(D)$ are transformations of one another, For f(D) fitting: is given by the inverse of the volume of air (V). if drop terminal velocity – size relation v(D) is known. CDF is computed with the Weibull plotting position formula

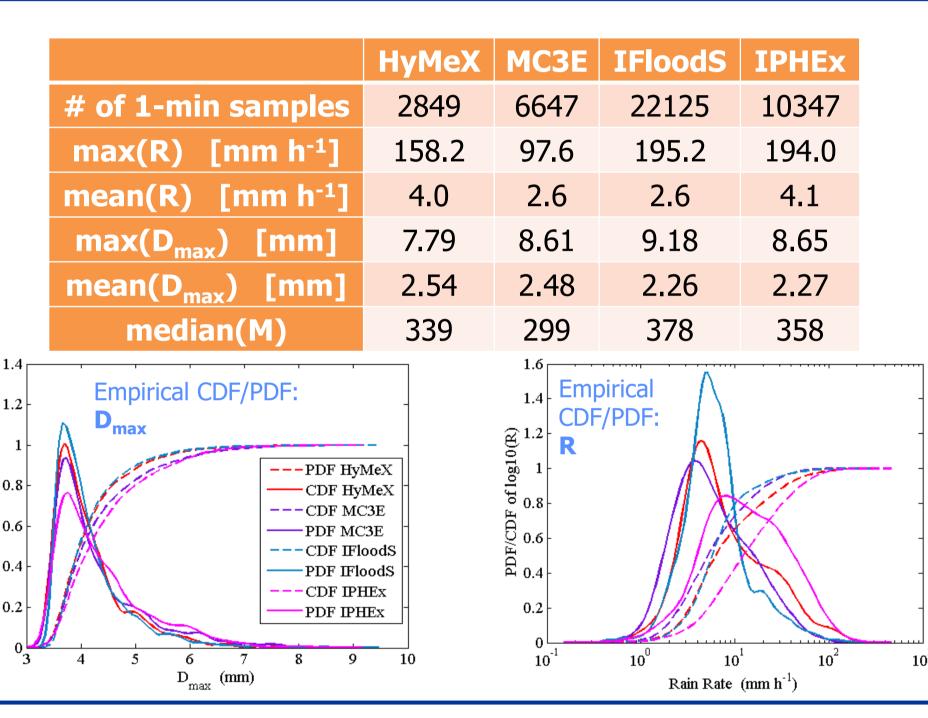
2DVD
Contraction of the second s

2D videodisdrometer The (2DVD) optical ĪS an that measures disdrometer the equivolumetric diameter and fall velocity of each single falls hydrometeor that through its virtual measuring area.

Thousands of 1-minute drop spectra were collected by NASA 2DVDs in four pre-launch field campaigns of Ground Validation program of NASA/JAXA Global Precipitation Measurement (GPM) mission

Experimental data





Results

<u>**Rejection rate from KS test (all datasets)**</u>

	Fitting of $f(D)$						Fitting of $f_v(D)$				
	HyMeX	MC3E	IFloodS	IPHEx			HyMeX	MC3E	IFloodS	IPHEx	
gamma	69.0%	66.2%	71.8%	67.0%		gamma	77.3%	73.9%	83.7%	76.7%	
lognormal	69.8%	69.6%	80.0%	73.5%		lognormal	81.3%	78.9%	88.9%	82.3%	
Weibull	81.6%	78.4%	79.5%	78.0%		Weibull	85.5%	82.2%	85.9%	82.3%	

Success rate (all datasets)

Percentage of samples that have passed the KS test and best fitted by a model (distribution with maximum log-likelihood value is the one that performs best). Completed ML is shown because of negligible differences with truncated ML.

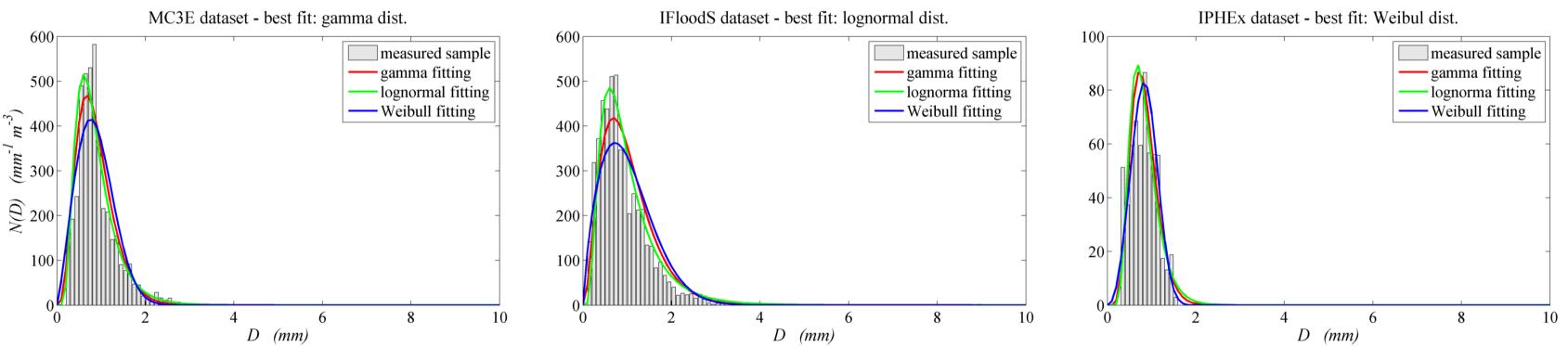
	Fitting of $f(D)$						Fitting of $f_v(D)$				
	HyMeX	MC3E	IFloodS	IPHEx			HyMeX	MC3E	IFloodS	IPHEx	
gamma	22.1%	22.0%	21.0%	22.8%		gamma	15.8%	16.7%	11.5%	16.0%	
lognormal	14.3%	15.1%	8.1%	10.7%		lognormal	10.7%	12.7%	5.3%	8.0%	
Weibull	9.9%	11.6%	12.2%	13.8%		Weibull	7.3%	8.6%	8.6%	11.1%	
none	53.6%	51.3%	58.8%	52.6%		none	66.2%	62.0%	74.6%	64.9%	

✓ For $f_{\nu}(D)$ fitting, the gamma distribution is the best ...

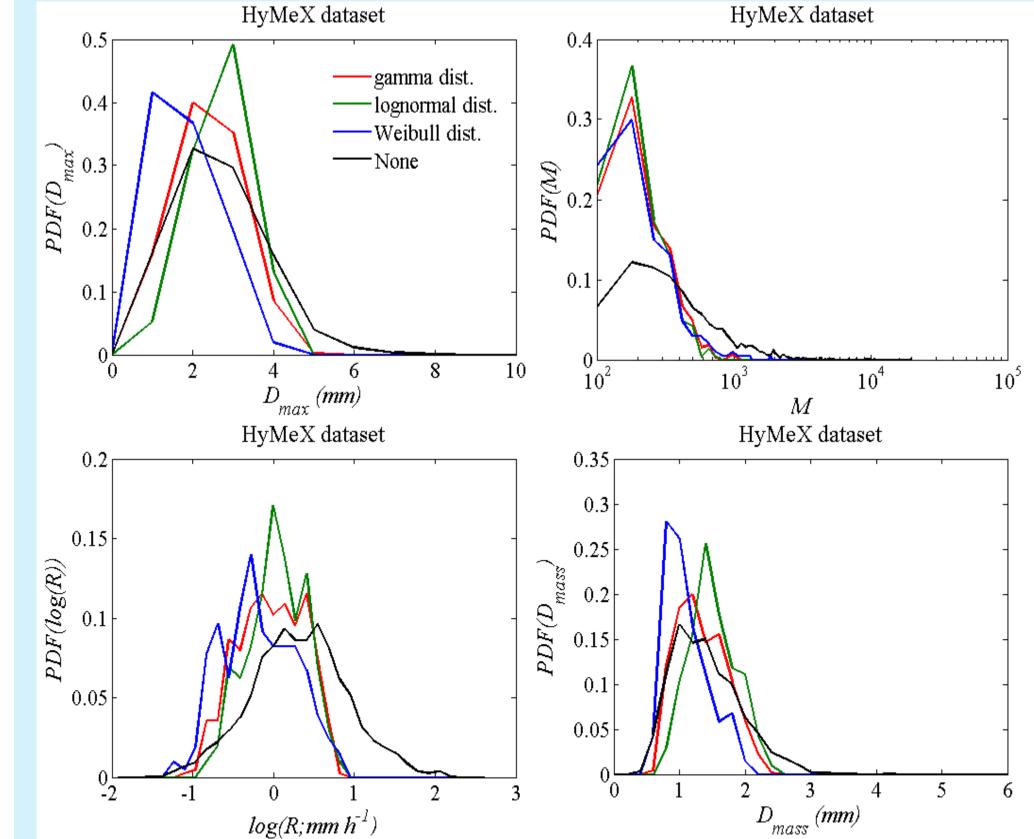
 \checkmark but there is a number of samples that are best fitted by a heavy-tailed distribution (i.e. lognormal distribution).

Percentage of samples that cannot be represented

Example of measured 1-min. sample along with the three fitted distributions



Conditions leading a model to overcome the others



- $\checkmark D_{max}$, R, and D_{mass} , shown a dependence on the selected best model:
 - The lognormal distribution (heavy-tailed) represents better samples with high D_{max} R, and D_{mass};
 - the opposite is valid for the Weibull distribution (a lighttailed distribution).
- \checkmark The number of drops in 1 minute (M) does not affect the selection of the best model
- For large *M*, none of the model

<u>represented by any of the three models (all datasets)</u>

 \checkmark In $f_{\nu}(D)$ fitting, for ~65% of the drop spectra the KS test rejects all the selected models. ✓ This high rejection rate car

In $f_v(D)$ fitting, for ~65%		Fitting of $f_v(D)$				
of the drop spectra the KS		HyMeX	MC3E	IFloodS	IPHEx	
test rejects all the selected	M < 200	39.6%	42.0%	52.0%	39.5%	
models.	200 ≤ M < 500	61.4%	59.9%	69.1%	56.1%	
This high rejection rate can	500 ≤ M < 1000	89.8%	85.8%	91.0%	83.7%	
be justified by the large	1000 ≤ M < 2500	98.0%	98.6%	99.0%	98.2%	
sample size (M).	M > 2500	100%	100%	100%	100%	

is adequate to fit the data The same happens also for smaller *M* in a significant number of cases

More in: Adirosi, E., Baldini, L., Lombardo, F., Russo, F., Napolitano, F., Volpi, E., Tokay, A. (2015). Comparison of different fittings of drop spectra for rainfall retrievals. Advances in Water Resources, 83, 55-67.

Adirosi, E., Lombardo, F., Volpi, E, Baldini, L., (2016). Raindrop size distribution: Fitting performance of common theoretical models, Advances in Water Resources, 96, 290-305,.

