

ALOS / PaLSAR Pol-InSAR for Forest Height Estimation : Potential and Limitations

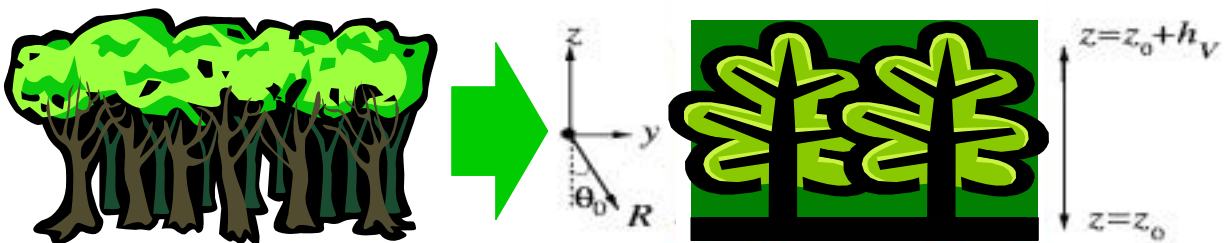
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Random Volume over Ground (RVoG) Scattering Model



$$\tilde{\gamma}(\hat{w}^p) = \exp(i\varphi_0) \frac{\tilde{\gamma}_V + m(\hat{w}^p)}{1 + m(\hat{w}^p)}$$

Volume Coherence:

$$\tilde{\gamma}_V = \frac{I}{I_0}$$

$$I = \int_0^{h_V} \exp(ik_z z') \exp\left(\frac{2\sigma z'}{\cos\theta_0}\right) dz'$$

$$I_0 = \int_0^{h_V} \exp\left(\frac{2\sigma z'}{\cos\theta_0}\right) dz'$$

4 Parameters:

Volume height h_V

Extinction σ

Topography φ_0

Interferometric Coherence:

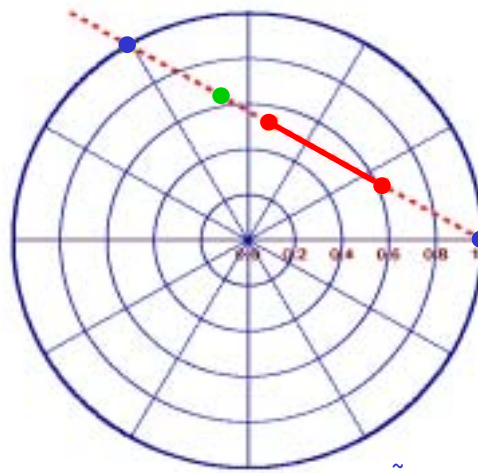
$$\tilde{\gamma}(\omega^p) = \exp(i\phi_0) \frac{\tilde{\gamma}_V + m(\omega^p)}{1 + m(\omega^p)}$$



$$\tilde{\gamma}(\omega^p) = \exp(i\phi_0) \left[\tilde{\gamma}_V + \frac{m(\omega^p)}{1 + m(\omega^p)} (1 - \tilde{\gamma}_V) \right]$$

$$\tilde{\gamma}(\omega^p) = \exp(i\phi_0) [B + X(\omega^p) A]$$

Equation of a straight line in the complex plane !!!



$\tilde{\gamma}(m = \infty)$

- Line Slope := f (Baseline, Vegetation Height, and, Extinction)

- Line Length := f (Baseline, Vegetation Height, Extinction, and, Ground Scat. Amplitude)

Frequency Dependent Parameters

The optimal polarisations represent the limiting points of the "visible" line part



Random Volume over a 2-dim Surface



Assumption: The ground is a 2-dimensional scatterer



There is a polarisation where the ground is not visible (not necessarily the HV polarisation)

1st Opt. Coherence: $\tilde{\gamma}_1(\omega_1^p) = \exp(i\phi_0) \frac{\tilde{\gamma}_V + m_1(\omega_1^p)}{1 + m_1(\omega_1^p)}$

$$m_1(\omega_1^p) < \infty$$

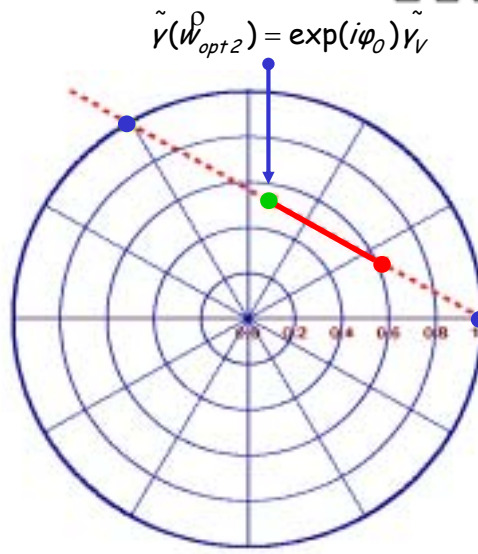
2nd Opt. Coherence: $\tilde{\gamma}_2(\omega_2^p) = \exp(i\phi_0) \tilde{\gamma}_V$

$$m_2(\omega_2^p) = 0$$

3rd Opt. Coherence: $\tilde{\gamma}_3(\omega_3^p) = \exp(i\phi_0) \frac{\tilde{\gamma}_V + m_3(\omega_3^p)}{1 + m_3(\omega_3^p)}$

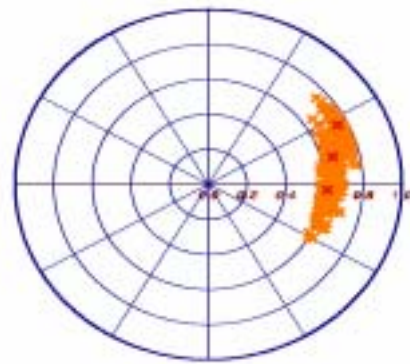
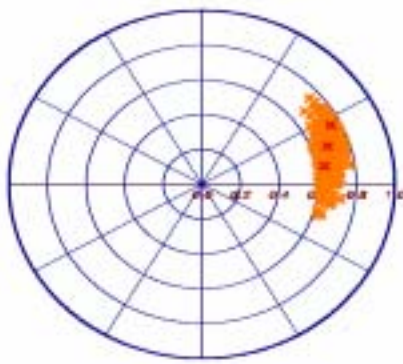
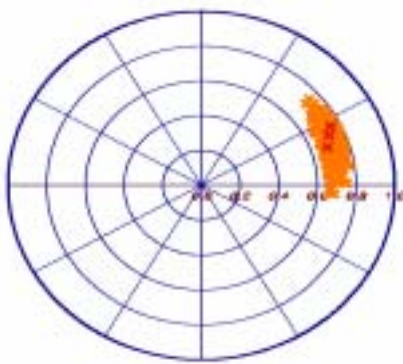
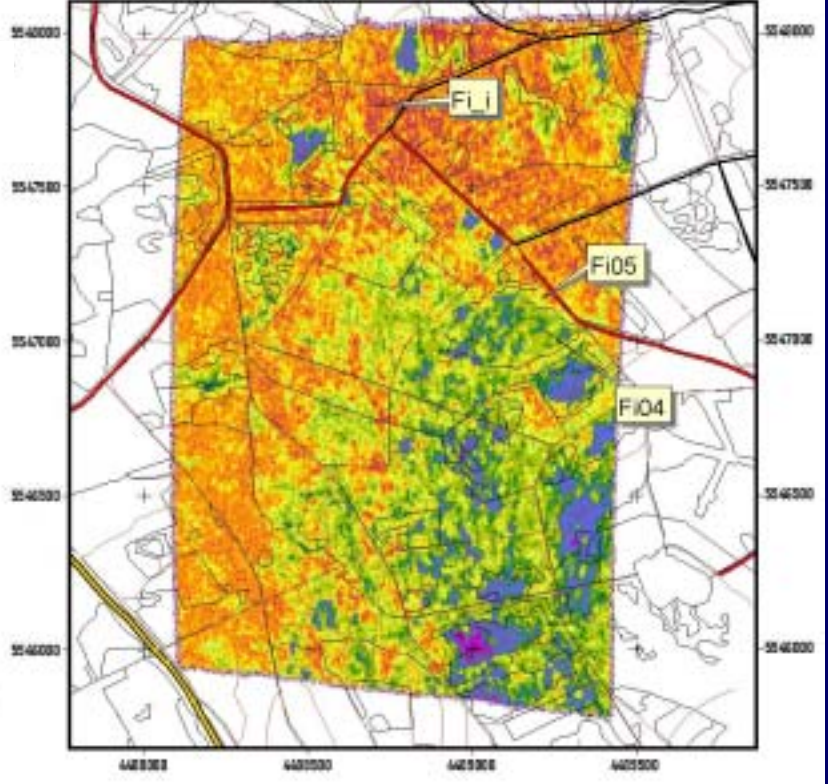
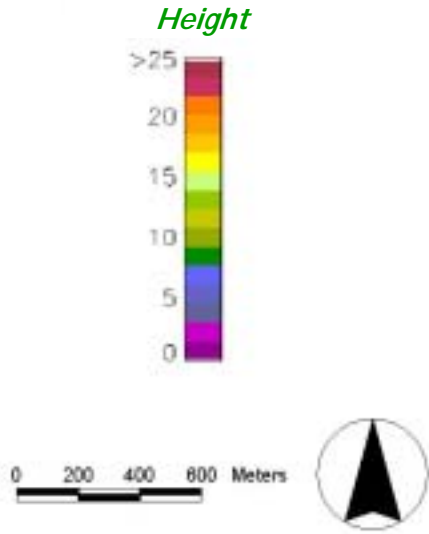


Unique solutions for all five parameters:



$$\tilde{\gamma}(\omega_{opt2}^p) = \exp(i\phi_0) \tilde{\gamma}_V$$

*Forest Height Map
Fichtelgebirge Test Site*



Pol-InSAR Lite: HH or VV and HV



Assumption: The ground is a 2-dim scatterer in HH-VV Sub-space



In HV the ground is not visible

HH (or VV) Coherence: $\tilde{\gamma}_{HH}(\tilde{w}_{HH}^D) = \exp(i\varphi_0) \frac{\tilde{\gamma}_V + m(\tilde{w}_{HH}^D)}{1 + m(\tilde{w}_{HH}^D)}$

$0 < m(\tilde{w}_{HH}^D) < \infty$

HV Coherence: $\tilde{\gamma}_{HV}(\tilde{w}_{HV}^D) = \exp(i\varphi_0) \tilde{\gamma}_V(h_V, \sigma)$

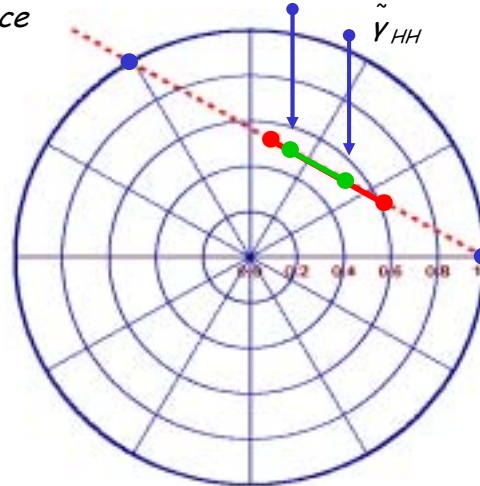
$m(\tilde{w}_{HV}^D) \stackrel{!}{=} 0$



The two points allow (in principle) to estimate the line and to resolve the RVoG problem



Unique solutions for: Volume height h_V , Extinction σ and Topography φ_0

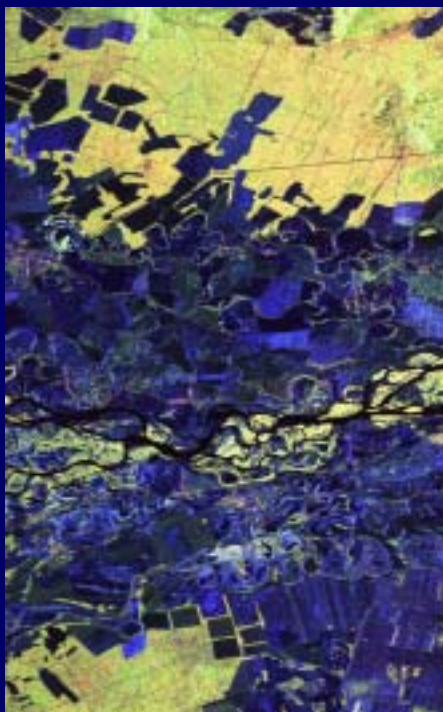
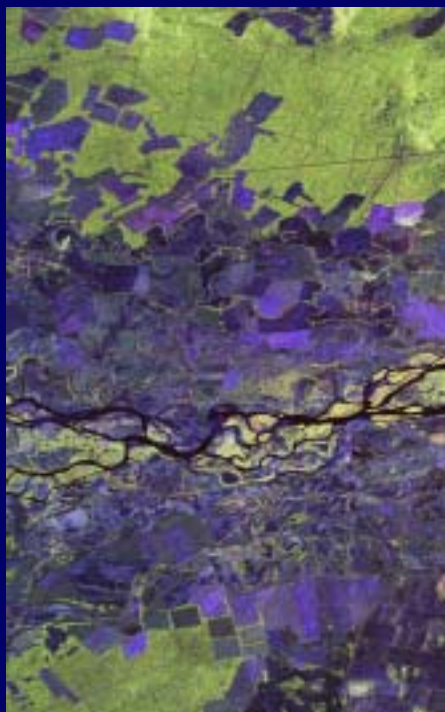


Pauli Images



Temporal Baseline: 48 Hours

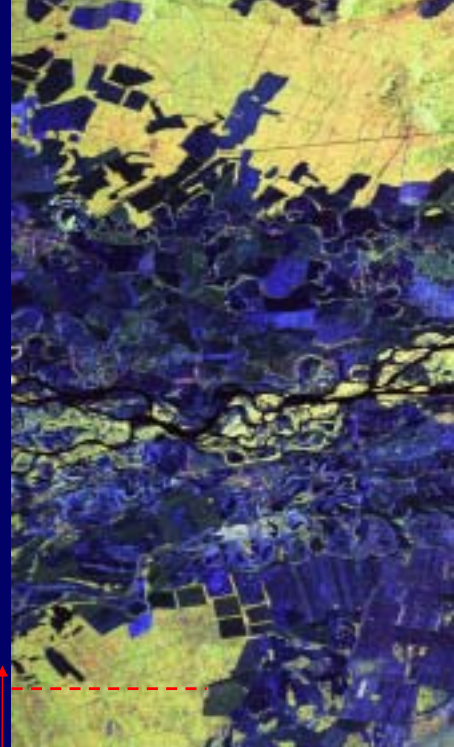
SIR-C / Test Site: Kudara, Russia



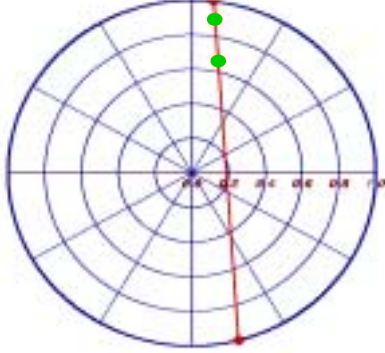
RGB-Coding

HH-VV

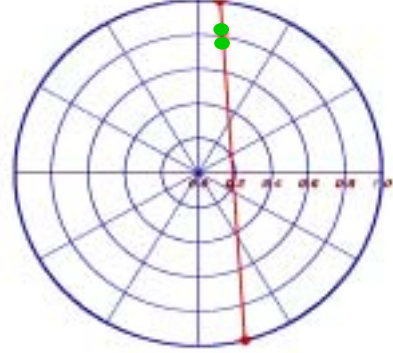
2HV



Range L-band



Quad-Pol



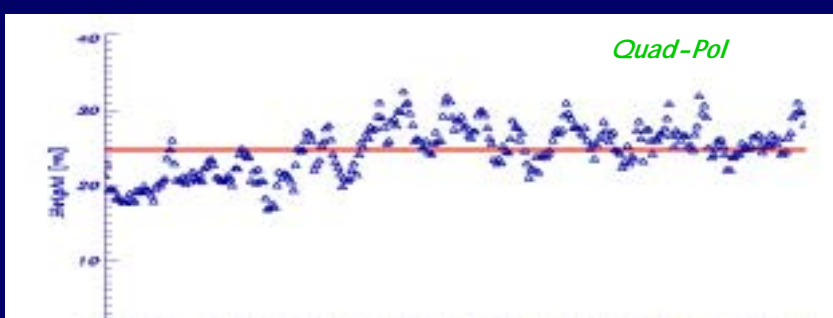
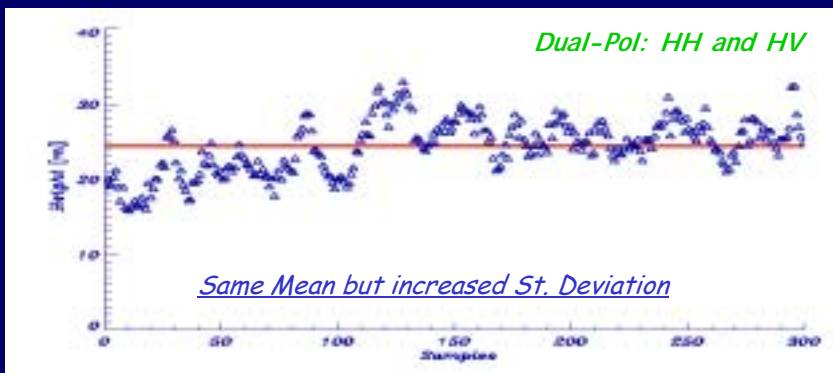
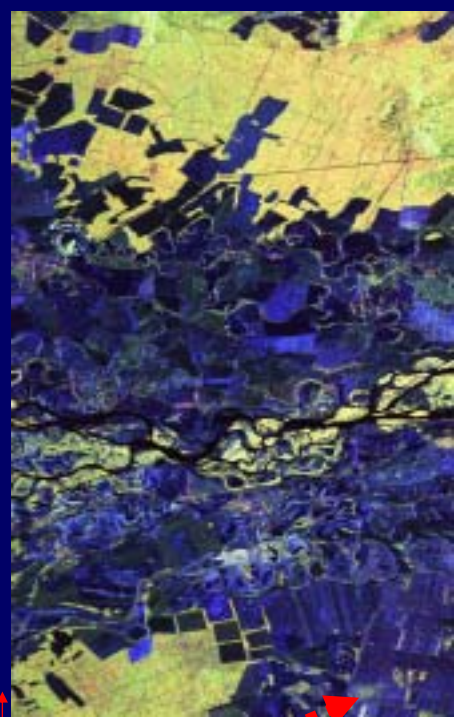
Dual-Pol (HH-HV)

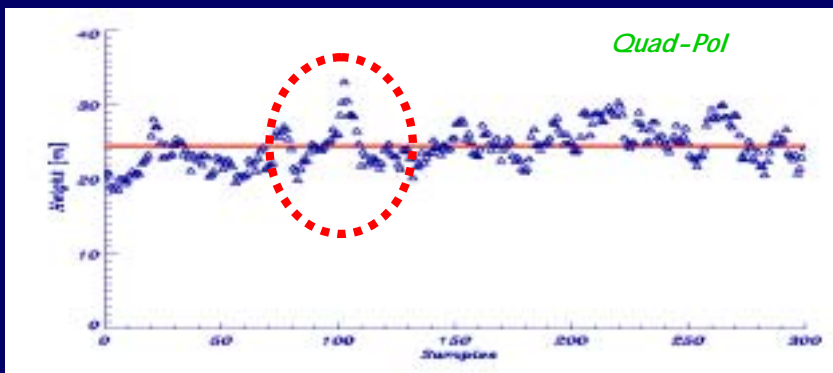
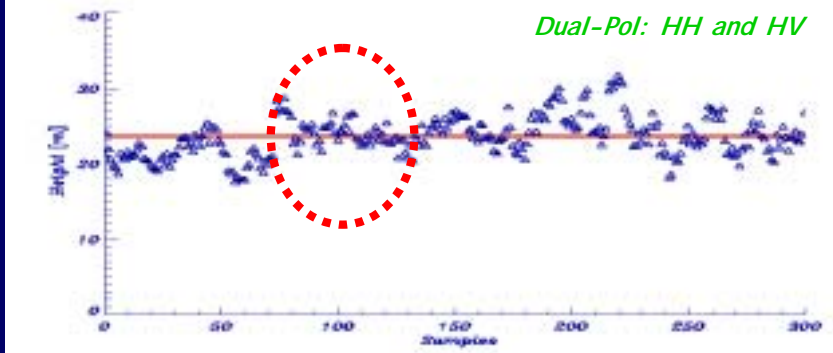
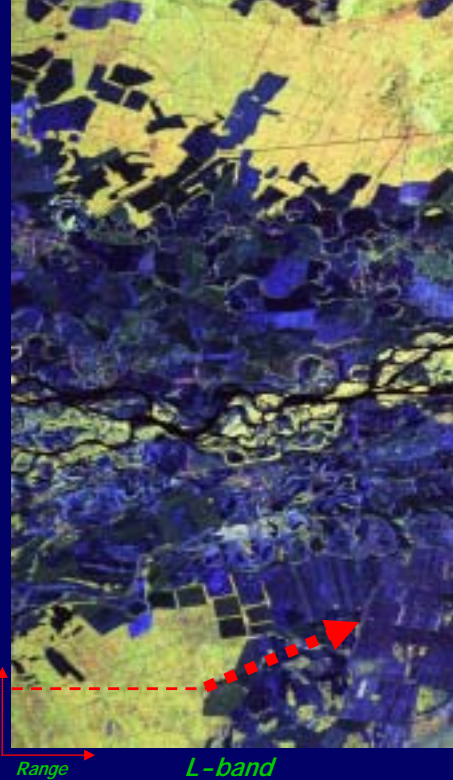


Forest Height Estimation: Quad-Pol vs. Dual-Pol

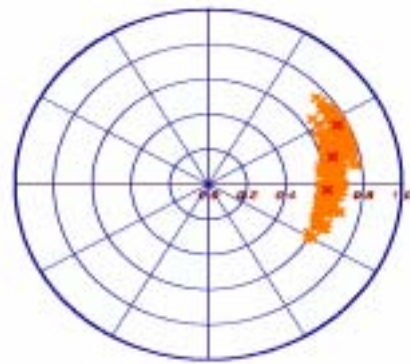
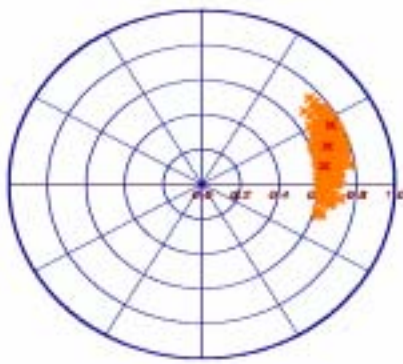
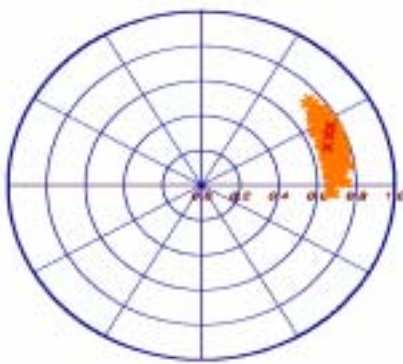


SIR-C / Test Site: Kudara, Russia





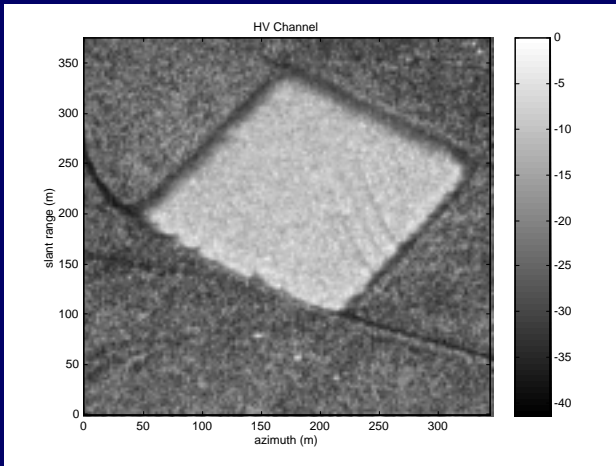
Temporal Baseline: 48 Hours



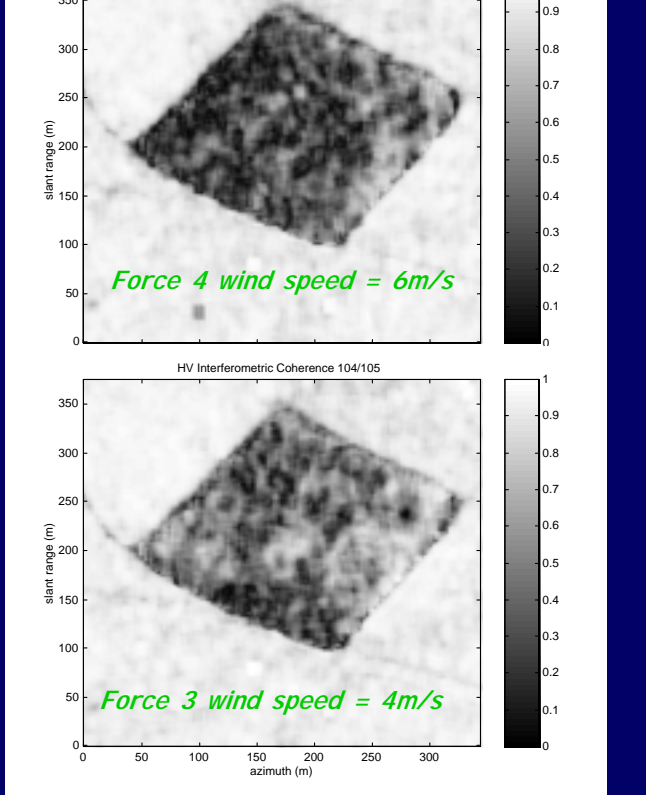
Temporal Decorrelation



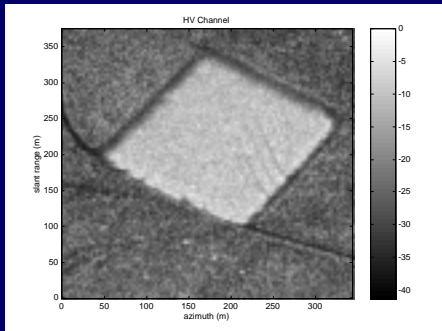
E-SAR / Test Site: Fox Covert, England



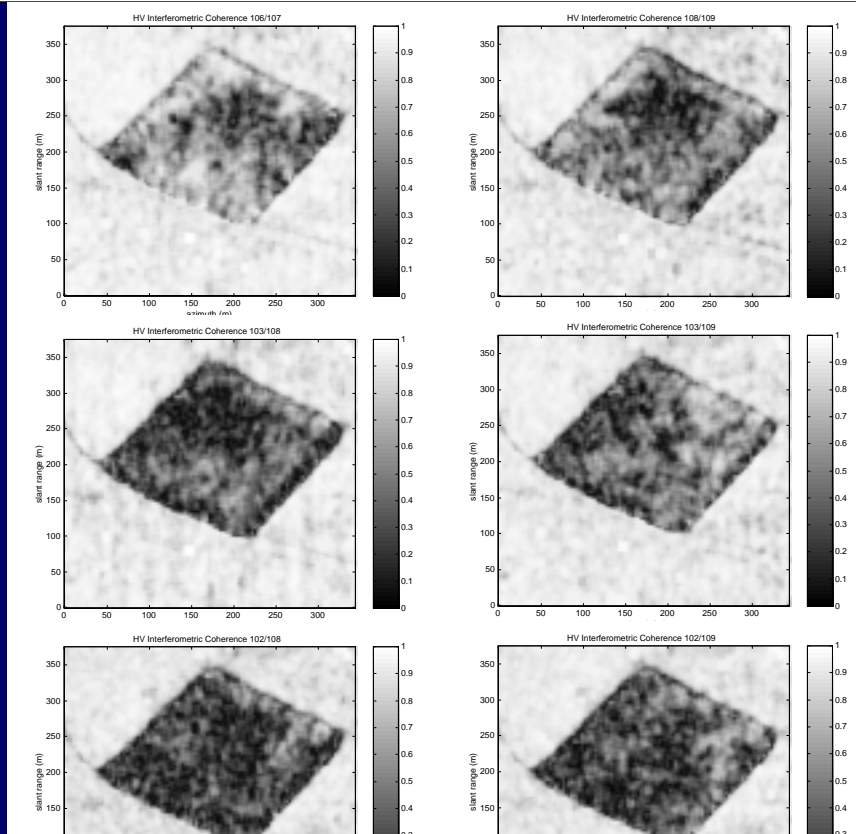
L-band HV Image



E-SAR / Test Site: Fox Covert, England



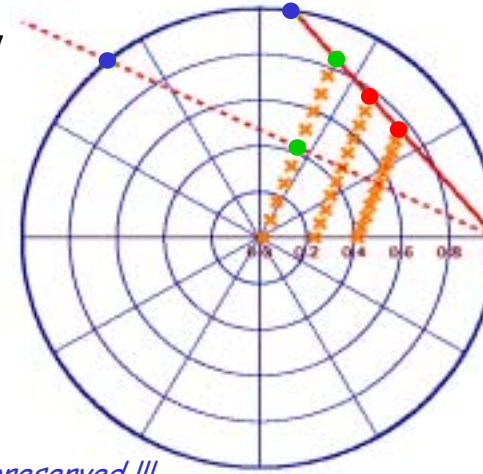
L-band





The 2nd order polarimetric properties of the ground [T_G] and the volume scatterer [T_V] remain the same:

- Ground / Volume amplitude ratios $m(\hat{w})$ are unaffected
- $0 \leq \gamma_T \neq f(m(\hat{w})) \leq 1$ is equal for all polarisations !!!



Interferometric Coherence: $\tilde{\gamma}(\hat{w}) = \exp(i\varphi_0) \frac{\gamma_T \tilde{\gamma}_V + m(\hat{w})}{1 + m(\hat{w})}$



$$\tilde{\gamma}(\hat{w}) = \exp(i\varphi_0) \left[\gamma_T \tilde{\gamma}_V + \frac{m(\hat{w})}{1 + m(\hat{w})} (1 - \gamma_T \tilde{\gamma}_V) \right] \quad \text{the line is preserved !!!}$$

- γ_T affects slope of the line but not the position of the points on the line.
- φ_0 remain invariant under variations of γ_T . The estimation of φ_0 is still possible !!!
- γ_T leads to an underestimation of $\tilde{\gamma}_V$ and thus a overestimation of volume height.

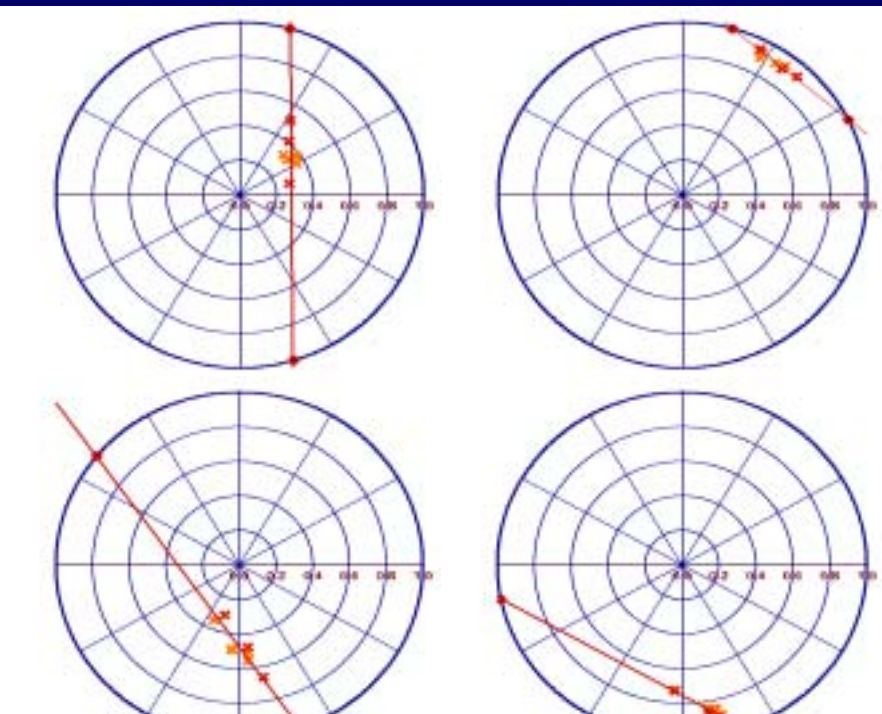
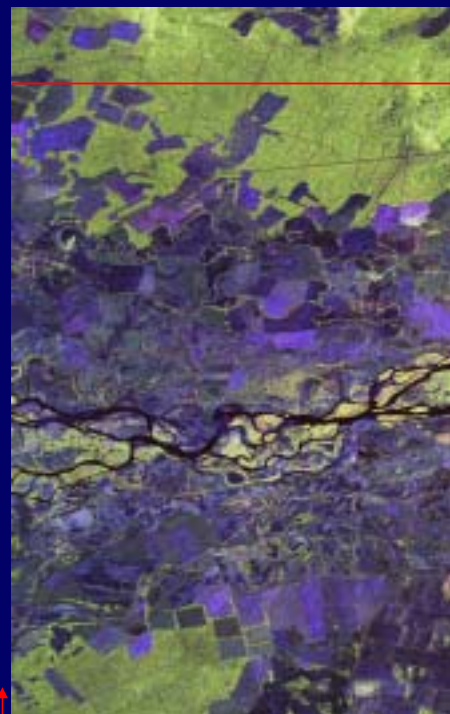


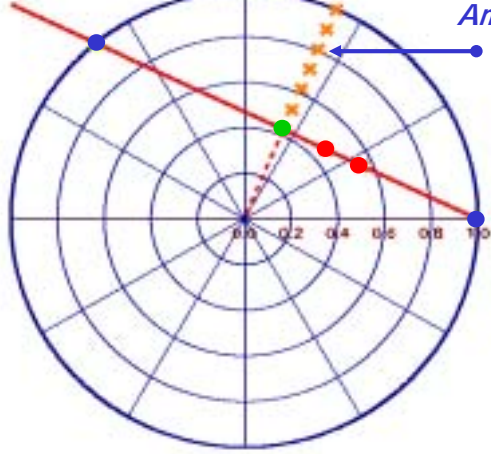
Line Comparison: C-Band vs. L-Band



Temporal Baseline: 24 Hours

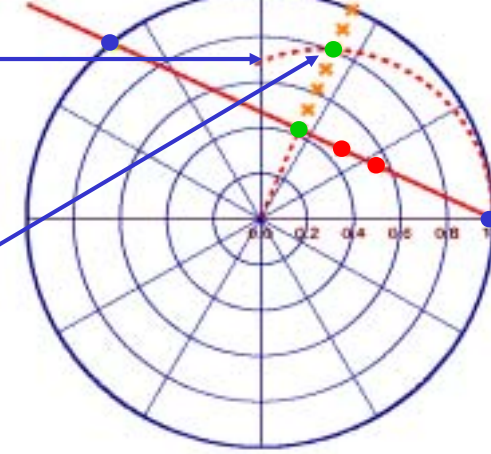
SIR-C / Test Site: Kudara, Russia





Ambiguity area

Line of ct. extinction



$\exp(i\varphi_0)\tilde{\gamma}_V$

Volume Height Estimation:

- Assumption of the mean extinction value
- Estimate the corresponding $\tilde{\gamma}_V$ value

$$\tilde{\gamma}_V = \frac{\int_0^{h_V} \exp(i k_z z') \exp\left(\frac{2 \sigma z'}{\cos \theta_0}\right) dz'}{\int_0^{h_V} \exp\left(\frac{2 \sigma z'}{\cos \theta_0}\right) dz'} \rightarrow h_V$$

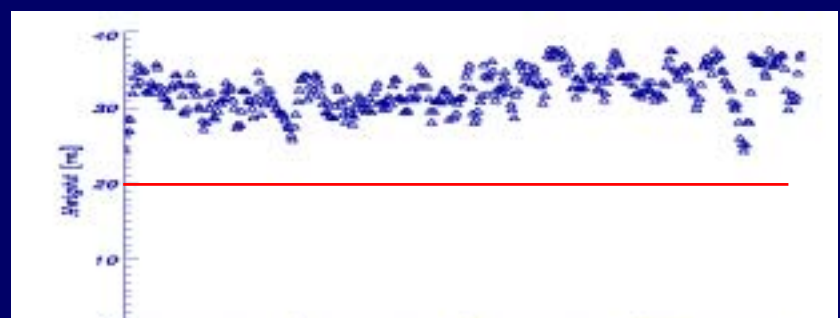
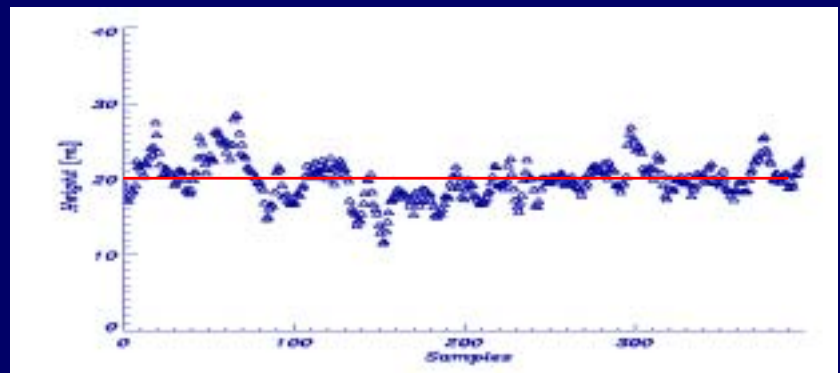
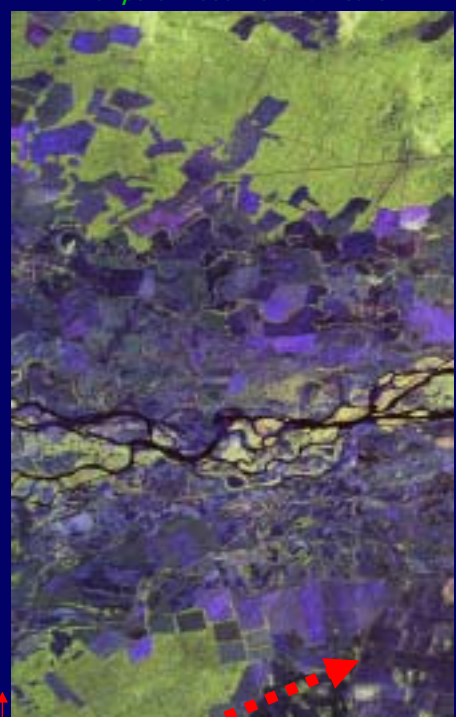


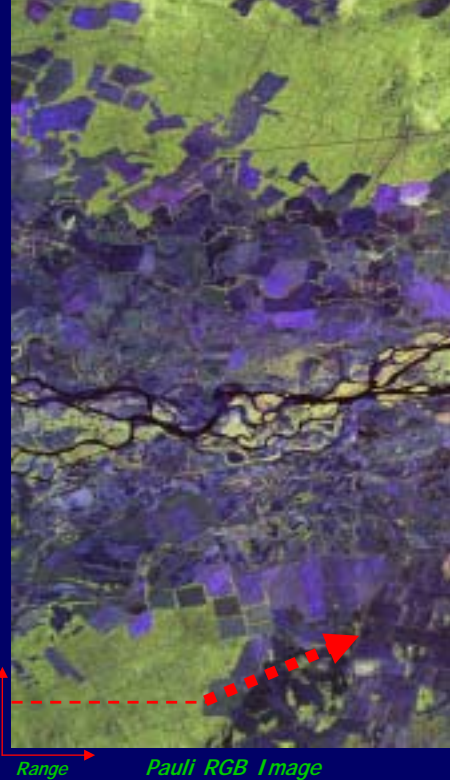
Forest Height Estimation: C-Band vs. L-Band



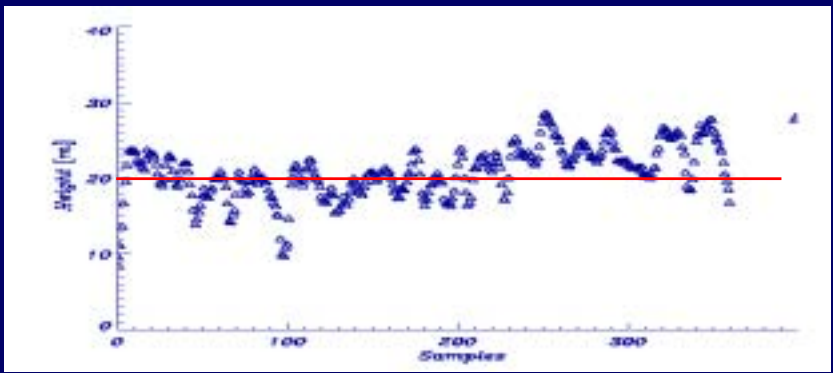
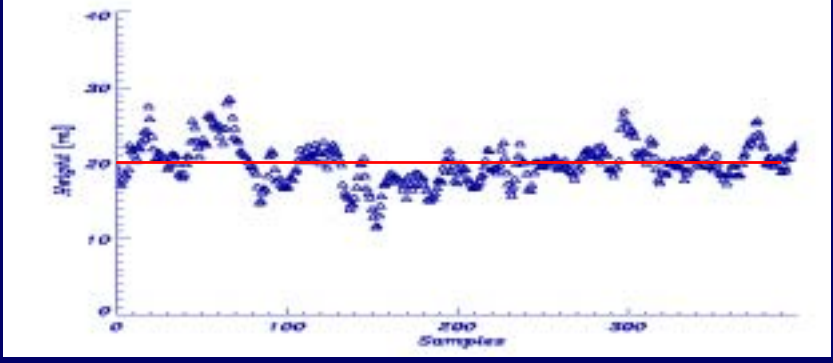
Temporal Baseline: 24 Hours

SIR-C / Test Site: Kudara, Russia





Range Pauli RGB Image



Conclusions



- *Unbiased estimation of forest height and underlying topography is in principle possible in a dual-pol (HH or VV and HV) Pol-InSAR scenario.*
- *The estimation accuracy is expected to drop especially in terrain with topographic variations. The availability of a DEM may be advantageous.*
- *Temporal decorrelation makes - in general - accurate unbiased parameter inversion impossible.*
- *Moderate temporal decorrelation of the volume layer can be accounted in the RVoG inversion model and compensated.*
- *However additional regularisation is required in order to obtain unique estimates.*
- *The availability of multiple-baselines (temporal and spatial) may allow a more flexible / accurate regularisation and is a serious option for increasing est. accuracy*